

C Software Formal Verification

Review, challenges and future directions

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Abstract—This paper reviews briefly the literature on formal verification of C software. Most existing C software model checkers and automatic theorem provers deal well only with small size code C software. Furthermore, full mechanization of conventional techniques to reduce the verification process complexity as code summation and abstract interpretation is merely impossible. Another challenge is how to choose the most suitable tool(s) among a panoply of available tools. We think that Artificial Intelligence can mitigate the above problems. For instance, by applying machine learning algorithms, the verification tool can automatically infer properties to be checked and synthesize proofs.

Keywords-C software; formal verification; Artificial Intelligence

I. INTRODUCTION

The debut of research works on mathematical reasoning about imperative programs goes mainly back to the works of Floyd [13] and Hoare on the logics of axioms (Hoare logic) [17], the works of Dijkstra on weakest preconditions calculus [8, 9] and abstract interpretation [6]. In the same context, we find other former works that tried to formalize and check imperative programs using type systems [11] and algebraic semantics [14]. Since that, many extensions and logics have been developed to reason about arrays, complex and dynamic typed data structures, unbounded loops, floating-point arithmetic, recursive functions, and concurrency. Separation logic [28], matching logic [35], dependent type theory [36], and refinement types [15] are among such extensions. Remarkable advances in SMT solvers technology have enhanced the automation level of both theorem provers and model checkers. Actual theorem provers and model checkers use SMT solvers as backend helpers and other frontend tools to reduce and simplify the verification process. Recent works indicate that the verification of low-level systems code as OS kernel has become tractable.

As it is known, the C language is still very popular programming language due to its great flexibility in terms of data representation and pointers arithmetic. C has been used to implement operating systems kernels and embedded systems. The majority of software in embedded systems is still written in C. C code can also be used to automatically generate a HDL (Hardware Description Language) code, which will be used later in embedded system hardware part synthesis. However, C is weak-typed (i.e. C's types provide no invariants about data values) and sometimes ambiguous. C standard [19] defines the

C memory model as a sequence of bytes (i.e. untyped memory model) and underspecifies the semantics of the C language. Furthermore, the uncontrolled use of I/O library functions can easily create security vulnerabilities. In order to minimize the number of bugs in C code, some solutions emphasize what we call standards-based development. These standards (example MISRA) impose a set of obligations and constraints on coding. For instance, the non-use of side effect statements or pointers [29]. Despite, this solution seems useful, it constraints the programmer creativity and minimizes optimization opportunities of the C code. In addition, most of these obligations are just guidelines that lack systematization and automatization. Producing correct imperative code can be the fruit of the correct-by-construction design approach. In this approach, code can be automatically synthesized through a sequence of refinements of an abstract formal specification. Each refinement must be proved correct with respect to the previous one. Consequently, the generated code implements correctly its specification. The method B follows this approach. In contrast to functional programs, imperative programs proving is more challenging. Indeed, it is not obvious, whether the well-known Curry-Howard correspondence [16] which links a functional program to its equivalent logical proof system can be naturally applied for imperative programs. Imperative languages include some uncommon constructors for mathematical logics as pointers, global variables, and so on. This makes reasoning about imperative programs in general a non-trivial task.

On the other side, Artificial Intelligence (AI) is becoming more attractive since it can offer some powerful tools to boost the formal verification process. Our aim through this paper is first to review shortly the literature, then to define the main challenges and finally to shine the spotlight on some promising future directions in particular the synergy between software formal verification and AI. This paper is structured as follows: Section 2 is devoted to the state of the art on C software formal verification. In this context, we present a set of criteria to compare between existing approaches and tools. In section 3, we pass quickly on the main challenges and in section 4 we discuss some possible future directions before concluding.

II. LITERATURE REVIEW

The first initiative in the C language formalization returned back to the work of Sethi [31] where a denotational semantics of a subset of the ANSI C language was proposed. Despite, this

work was incomplete with respect to the ANSI standard, it gave a big push to subsequent researchers to investigate more in this topic. The literature on formal verification of C software is very rich, however, we can cite some pertinent works as in [1, 3, 5, 7, 18, 21, 26, 27, 30, 34, 35], and some interesting PhD and master thesis on the same topic as in [10, 20, 22, 25, 33]. Many code C formal verification tools exist. For a fair evaluation of such tools, Competition on Software Verification (SV-COMP) has been established [4]. The first edition was in 2012 and the last one in 2023. The competition includes 23 805 verification tasks for C programs to check four properties that are reachability, memory safety, overflows, and termination. The evaluation is performed based on a scoring schema that assigns points in function of the type of the reported result (unknown, false correct, false incorrect, true correct, true incorrect) for the given property. We can however classify these works according to a set of pertinent criteria. In this context, we propose a taxonomy based on ten criteria. These criteria include the application domain, the orientation of the software, the supported C language, the C memory model used, the intermediate representation, the formalization method, the logics used in the proofs, the verification method, the reduction technique, and the type of checked properties.

- The application domain, which can be general-purpose, compilers, cryptography, OS kernels, device drivers, hypervisors, embedded systems and robotics. It is important to recognize the application domain in order to choose the more appropriate formalism and verification technique. For example, device drivers and operating systems code uses pointers as first class and the code usually contain some fragments written in assembly code. In this case, the mathematical proofs have to formalize in addition to C code, the assembly code too. The type of properties to be proved may also dependent on the domain of application. For instance, C code that implement multi-tasks OS kernels have to guarantee the mutual exclusion and isolation properties and so on.
- The orientation of the software, which can be control-oriented, data-oriented or mixt. A typical control-oriented C software is composed of control statements (e.g. if else, or switch) operating on very small-sized data. On the other hand, data-oriented C software is composed of complex operations or treatments on large-sized data. Model checking is more suitable for control-oriented software with simple properties and theorem proving for data-oriented software with complex properties.
- The supported C language which can be the full ANSI standard, a subset of the standard (i.e. the full standard excluding some constructors or features), or a specific C sublanguage such as C0 and CoreC*.
- The C memory model (i.e. the heap model) which, can be un-typed (i.e. raw arrays of bytes), typed or hybrid. The untyped model adds significant annotation burden, and render the reasoning computationally expensive.

The typed model however, offers a reasonable abstraction level for verification.

- The intermediate representation of C code, which can be a restricted subset of the C language itself as CIL, LLVM-IR, an abstract model as the CFA (Control Flow Automaton), or an intermediate formal language as Simpl and Boogie. Compared to the original C code, the intermediate representation generally has fewer constructs and unambiguous syntax, which make formal verification easier.
- The formalization approach, which can be annotation-based approach, semantics-based approach, transformational approach, reverse engineering approach and the cooperation approach.

In the annotation-based approach, the original C source code is annotated by specification constructs. These logical annotations may specify functions pre-conditions and post-conditions, loop and type invariants, assertions and so on. From these annotations, verification conditions (VC) or obligations proofs are generated automatically using Hoare-style weakest precondition method and checked using an automatic or interactive theorem prover. Annotations can be burdensome for programmers especially if these annotations are expressed in an unfamiliar formal specification language. In order to overcome this issue, the C language was extended to support Design-by-contract paradigm giving the birth to ACSL (The ANSI/ISO C Specification Language). In the semantics-based approach, the semantics (i.e. operational or denotational semantics with possibly categories definition) of the C language or a substantial subset of it is explicitly defined in some formal specification language. The properties to be checked are also expressed in the same formal language. In the transformational approach, the source code is transformed either directly to another formal specification written in a certain formal language (e.g. transformation of C imperative code to a purely functional code in ML as done by the Why tool into the Coq assistant prover) or to an abstraction (i.e. predicate abstraction) of the original code in the same language (i.e. C). In the reverse engineering approach, the C source code is usually reversed automatically to a formal or a semi-formal model using UML. Then some formal checking is applied on this UML model to prove or refute the desired properties. The cooperation approach is any feasible sequential or concurrent combination of the above approaches.

- The logics and theories of the formal system and proofs. Those include Hoare, separation, rewriting and temporal logics, dependent and refinement types and category theory.
- The verification method that can be symbolic execution with its variants (static, dynamic), theorem proving with its variants (fully automatic, interactive proof assistants), model-checking with its variants to verify larger programs (with complex loops) or programs with infinite states (i.e. symbolic model checking, abstract

model checking, bounded model checking), SAT/SMT solving, or any feasible combination of them. For instance, symbolic execution often calls SAT/SMT solvers. Theorem provers, even model checkers may call SAT/SMT solvers to increase the automation level. A combination of model checkers and theorem provers is also possible. For example, in the Counter Example Guided Refinement approach, first the source program is abstracted away using predicate abstraction technique. A model checker working on this abstraction may check a certain property. If the property is not true, the model checker gives a counter example. In this case, a refinement step will be triggered during which a theorem prover can be called to check whether this counterexample reflects a true error in the program or just a spurious one due to abstraction. The theorem prover can call in turn a SAT or SMT solver to prove the satisfiability of a certain condition.

- The reduction technique used to reduce the complexity of the formal verification. Among these techniques, we find abstraction and program slicing. Abstract interpretation and predicate abstraction are the two common techniques used.
- The checked properties can be simple or complex including the functional correctness, the termination, reachability properties, safety and security properties. Safety may include static safety (i.e. type safety) or dynamic safety (i.e. memory safety). Security includes mainly confidentiality, integrity, and availability properties.

III. CHALLENGES

Despite the big efforts spent in boosting software formal verification process (e.g. exploring parallel and distributed formal verification, abstraction, modular and verification reuse), one can state that software formal verification in its current form cannot meet the needs of industrial sized C software in terms of performance, accuracy and scalability. With the ever increasing in the complexity of software functionalities and non-functional requirements, most state of the art and practice tools fail to formally prove the functional correctness in addition to non-functional properties as safety and security. Most users are unfamiliar with formal techniques and often find them hard to write formal specifications or proofs and even to use tools in particular theorem provers. Furthermore, the majority of available tools do not provide explanations in the case of proof failure and in the presence of a panoply of tools; the user is not able to choose the most suitable verification approaches and tools. The choice is a tradeoff between a set of conflictual criteria such as the amount of annotation effort, the automation level, the performance, the accuracy of results but more interestingly the soundness and the completeness of the proofs system.

IV. FUTURE DIRECTIONS

In order to increase the credibility of existing formal verification tools for large C software, researchers tend to

integrate some powerful promising technologies in particular AI, data mining, and quantum computing.

A. Artificial Intelligence and data mining

The idea of leveraging AI and data mining in formal verification has been attracted many researchers [2, 12, 24, 32]. In the context of software formal verification, we can apply AI with many flavors:

1. Automatic synthesis of formal proofs using machine learning algorithms.
2. Automatic inference of theorems and assertions as loop invariants and discovering pertinent properties for verification automatically.
3. Interactive aid of users to select the most suitable abstraction technique and the abstraction level.
4. Interactive assistance of users to choose the most appropriate formal approaches and tools using MCDM methods and tools integration.
5. Interactive support of users to select the most important parts in the software requiring formal verification and properties for checking since it is not feasible to formally verify the entire large software against all properties.
6. Using AI optimization meta-heuristics as genetic algorithms for example to guide the search process in model checking.
7. Integration of explication in the formal verification process and automatic repair of software vulnerabilities.
8. If the software code is supported with some informal specification expressed in natural language, NLP methods can be used to automatically or semi-automatically generate a formal specification and test cases. The latter can be used to complement the formal verification. Testing remains an efficient technique to discover compiler and hardware bugs.
9. AI can be used to automatically restructure the code software following the standards-based development approach to simplify the formal verification.

10. Benchmarking the C software formal verification processes, reuse and sharing the knowledge.

B. Quantum computing

Quantum computing emerged as a very powerful technology inspired from mechanics quantum theory. Due to the superposition and entanglement principles, researchers expect super polynomial speedup for big algorithms including formal verification algorithms. This paradigm however, still needs special algorithms to reduce noise because they do not have enough qubits to execute quantum error correction [23].

V. CONCLUSION

C software formal verification is hot research topic and a grand practical challenge. We can observe that C software formal verification has evolved over decades starting from former works focusing on the definition of a formal semantic of

the C language, the use of Hoare logic and automatic theorem provers ending by the use of more expressive logics and mathematical theories such as separation logic and refined types and the usage of model checkers and SMT solvers. Unfortunately, most existing approaches and tools suffer from many obstacles prevent them from being widespread in the industry. Finally, most researchers and experts have emphasized on formal verification process rethinking by making it AI-powered to boost the performance and the accuracy and enables tools integration and scalability. As short-term perspective, we plan to apply machine learning and in particular deep learning to automatically infer loops invariants and properties to be checked in a C program with nested loops and recursive functions.

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